

Course：Biostatistics
Level：Forth

## The Final Exam of the Second Semester 2020／2021

## The First Question：－

 （20 degree）1）Fill in the table given below．Answer the following questions．
a．Find the values：A，B，C，D．
b．Find the true class interval for the first class．

| Class <br> Interval | Freguency | Cumulative <br> Frequency | Relative <br> Frequency | Cumulative <br> Relative <br> Frequency |
| :---: | :---: | :---: | :---: | :---: |
| $5-9$ | 8 |  |  |  |
| $10-14$ | 15 |  | $C$ |  |
| $15-19$ | 11 | $B$ |  | $D$ |
| $20-24$ | $A$ | 40 | 0.15 |  |

c．Find the number of observations less than 19.5
2）A company has two sections with 40 and 65 employees respectively．Their average weekly wages are $\$ 450$ and $\$ 350$ ．The standard deviation are 7 and 9 ．Which section has larger variability in wages？

## The Second Question：－（20 degree）

Suppose that we have two events $A$ and $B$ such that，$P(A)=0.4, P(B)=0.5, P(A \cap B)=0.2$ ．Find：

$$
P(A \cup B), P\left(\mathrm{~A}^{c} \cap \mathrm{~B}\right), P\left(\mathrm{~A}^{c} \cap \mathrm{~B}^{c}\right), P\left(\mathrm{~A}^{c} \mid \mathrm{B}\right), P(B \mid \mathrm{A}) .
$$

## The Third Question：（20 degree）

Suppose that $25 \%$ of the people in a certain population have low hemoglobin levels．The experiment is to choose 5 people at random from this population．Let X be the number of people out of 5 with low hemoglobin levels．Find：
1）The probability distribution of $X$ ．
2）The probability that at least 2 people have low hemoglobin levels．
3）The probability that at most 3 people have low hemoglobin levels．
4）The probability that more than 5 people have low hemoglobin levels．
5）The expected number and the variance of people with low hemoglobin levels．
Ended questions ．．．With my best wishes Dr．Khaled Mahfouz

The Model Answer of the Final Exam $2020 / 2021$ Biostatistics - 4 th
The First Question.
(1) $a, A=\sigma, \quad B=29$

$$
\begin{array}{ll}
A=6, & B=29 \\
C=0.375, & D=0.725
\end{array}
$$

[b] The class Interval $4.5=9.5$
(c) The number of observation $\leqslant 19.5=29$

| Class | $F$ | $C F$ | $R F$ | $C R F$ |
| :--- | :---: | :---: | :---: | :---: |
| Interval |  |  |  |  |
| $5-9$ | 8 | 8 | 0.2 | 0.2 |
| $10-14$ | 15 | 23 | $C$ | 0.575 |
| $15-19$ | 11 | $B$ | 0.275 | 0 |
| $20-24$ | $A$ | 40 | 0.15 | 1 |

(2)

$$
\begin{aligned}
& C V_{1}=\frac{\sigma_{1}}{x_{1}} \times 100=\frac{7}{450} \times 100=1.56 \% \\
& C V_{2}=\frac{\sigma_{2}}{x_{2}} \times 100=\frac{9}{350} \times 100=2.57 \%
\end{aligned}
$$

The second Question:

$$
\begin{aligned}
& * P(A \cup B)=P(A)+P(B)-P(A \cap B)=0.4+0.5-0.2=0.7 \\
& * P\left(A^{C} \cap B\right)=P(B)-P(A \cap B)=0.5-0.2=0.3 \\
& * P\left(A^{C} \cap B\right)=P(A \cup B)^{c}=1-P(A \cup B)=1-0.7=0.3 \\
& * P\left(A^{c} \mid B\right)=\frac{P(A \cap B)}{P(B)}=\frac{0.3}{0.5}=0.6 \\
& * P(B \mid A)=\frac{P(A \cap B)}{P(A)}=\frac{0.2}{0.4}=0.5
\end{aligned}
$$

The Third Question:
Let $X_{i}$ the number of peaple duith law hemaglobin levels.
$\Rightarrow X \sim$ Binomial elistribution with $p=0.25, \quad n=5, \quad q=0.75$
(1) $f(x)=\binom{5}{x}(-0.25)^{x}(0.75)^{5-x}, \quad x=0,1,2, \ldots, 5$
(3) $P(x \geqslant 2)=1-(f(0)+f(1))=1-\left((0.75)^{5}+5(0.25)(0.75)^{4}\right)=0.367$
(3) $P(x \leqslant 3)=1-(f(4)+f(5))=1-\left[5(0,25)^{4}(0,75)^{5}+(0.25)^{5}\right]=0.984$
[4] $P(x>5)=0$
[5] $E(x)-n p=5\left(\frac{1}{4}\right)=1.2$

$$
\operatorname{Var}(x)=n p q=5\left(-\frac{1}{4}\right)\left(\frac{3}{4}\right)=\frac{15}{16}=0.9375
$$

